Oligomerization kinetics

Combined model

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Conclusion 000

Death Team Presents: A SCREEN PLAY A Mathematical Model of Apoptosis

Death Team

MBI 2007 Project Leaders: Baltazar Aguda and Chiu-Yen Kao

August 10, 2007

Conclusion 000

Outline

Introduction

- Background
- Motivation to model apoptosis
- Existing Models
- Novelties of our model
- 2 Analysis of caspase modules
 - Extrinsic C8/C3 module
 - Intrinsic C9/C3 module
- Oligomerization kinetics
 - DISC module
 - Apoptosome module
- ④ Combined model
 - Dynamical equations
 - Simulation results
- 5 Conclusion

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Introduction-Trailers Background: The directors and actors

Directors (Project Leaders)

- Baltazar Aguda
- Chiu-Yen Kao



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Introduction-Trailers Background: The directors and actors

Directors (Project Leaders)

- Baltazar Aguda
- Chiu-Yen Kao

Actors in order of appearance (Death Team)

- Heather Harrington Imperial College London
- Samik Ghosh University of Texas at Arlington
- Kenneth Ho California Institute of Technology
- K.C. Tung UT Southwestern Medical Center



Oligomerization kinetics

Combined model

Conclusion

Introduction-Trailers Background: The directors and actors



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Introduction 000000000000000000000000000000000000	Analysis of caspase modules	Oligomerization kinetics	Combined model	Conclusion
Introduct Background:	ion-Trailers What is apoptosis?			

• The development and maintenance of homeostasis in multi-cellular organisms arises from a complex interplay of cellular processes.

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Introduction 0000000000	Analysis of caspase modules	Oligomerization kinetics	Combined model	Conclusion
Introdu	ction-Trailers			
Background	I: What is apoptosis?			

 The development and maintenance of homeostasis in multi-cellular organisms arises from a complex interplay of cellular processes.

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What is Apoptosis?

Apoptosis, or programmed cell death is one of the key physiological mechanisms employed by the cell.

Introduction 000000000000000000000000000000000000	Analysis of caspase modules	Oligomerization kinetics	Combined model	Conclusion
Introduct Background: \	ion-Trailers What is apoptosis?			

• The development and maintenance of homeostasis in multi-cellular organisms arises from a complex interplay of cellular processes.

What is Apoptosis?

Apoptosis, or programmed cell death is one of the key physiological mechanisms employed by the cell.

• What distinguishes apoptosis from other types of cell death?

• The development and maintenance of homeostasis in multi-cellular organisms arises from a complex interplay of cellular processes.

What is Apoptosis?

Background: What is apoptosis?

Apoptosis, or programmed cell death is one of the key physiological mechanisms employed by the cell.

• What distinguishes apoptosis from other types of cell death?

A hallmark of the apoptotic process is its "programmed" nature

i.e. it is characterized by a controlled sequence of

well-defined steps which results in cell

destruction.

Oligomerization kinetics

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Conclusion 000

Introduction Background: Implications of apoptosis

- In the adult human body, several thousands of cells are regulated by mitosis and apoptosis continuously.
 - Formation of independent digits by massive cell death
 - Adult brain formation
 - Reproductive organ development

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Motivation to model apoptosis: Inappropriate cell decisions

 Inappropriate apoptosis may result in many physiological health problems.

Oligomerization kinetics

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Conclusion 000

Introduction Motivation to model apoptosis: Inappropriate cell decisions

- Inappropriate apoptosis may result in many physiological health problems.
- There are two possible outcomes:

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Motivation to model apoptosis: Inappropriate cell decisions

- Inappropriate apoptosis may result in many physiological health problems.
- There are two possible outcomes:

Insufficient apoptosis

In cancer cells, insufficient apoptosis leads to cell accumulation!

Oligomerization kinetics

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Introduction Motivation to model apoptosis: Inappropriate cell decisions

- Inappropriate apoptosis may result in many physiological health problems.
- There are two possible outcomes:

Insufficient apoptosis

In cancer cells, insufficient apoptosis leads to cell accumulation!

Excessive cell death

Various neurodegerative diseases (Parkinson's or Alzheimer's disease) are associated with excessive apoptosis.

Oligomerization kinetics

Combined model

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Conclusion

Introduction Motivation to model apoptosis: Significance

- Apoptosis also plays a significant part in immune system response.
- The apoptotic pathway is characterized by complex interactions.
- Scientists do not fully understand the entire pathway, key characteristics have been identified.

Oligomerization kinetics

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Conclusion 000

Introduction Motivation to model apoptosis: Significance

- Apoptosis also plays a significant part in immune system response.
- The apoptotic pathway is characterized by complex interactions.
- Scientists do not fully understand the entire pathway, key characteristics have been identified.
- We model to gain insight into the biological mechanisms at the cellular level

Oligomerization kinetics

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Introduction The Biology of Apoptosis: Caspases and signaling pathways

Why is death clean?

Death is clean due to proteases that degrade specific proteins during apoptosis.



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Oligomerization kinetics

Combined model

Conclusion

Introduction The Biology of Apoptosis: Caspases and signaling pathways

Why is death clean?

Death is clean due to proteases that degrade specific proteins during apoptosis.

What are Caspases?

Caspases (cysteine-containing aspartate-specific proteases) are enzymes involved in apoptosis. There are initiators and effector caspases.



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Oligomerization kinetics

Combined mode

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Introduction The Biology of Apoptosis: Schematic figure



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Oligomerization kinetics

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Conclusion 000

Introduction The Biology of Apoptosis: Signaling pathways

Oligomerization kinetics

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Conclusion 000

Introduction The Biology of Apoptosis: Signaling pathways

- Extrinsic (membrane receptor-mediated pathway)
 - Ligands bind to receptors to form DISC/FADD (death-inducing signaling complex).
 - DISC \rightarrow caspase 8 \rightarrow caspase 3 \rightarrow cell death.

Oligomerization kinetics

Combined model

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Introduction The Biology of Apoptosis: Signaling pathways

- Extrinsic (membrane receptor-mediated pathway)
 - Ligands bind to receptors to form DISC/FADD (death-inducing signaling complex).
 - DISC \rightarrow caspase 8 \rightarrow caspase 3 \rightarrow cell death.
- Intrinsic (mitochondria-mediated pathway)
 - BID or other stress cause mitochondria to release cytochrome c.
 - cytochrome c bind with Apaf-1 to form the apoptosome.
 - Apoptosome \rightarrow caspase 9 \rightarrow caspase 3 \rightarrow cell death.

Oligomerization kinetics

Combined model

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Introduction The Biology of Apoptosis: Signaling pathways

- Extrinsic (membrane receptor-mediated pathway)
 - Ligands bind to receptors to form DISC/FADD (death-inducing signaling complex).
 - DISC \rightarrow caspase 8 \rightarrow caspase 3 \rightarrow cell death.
- Intrinsic (mitochondria-mediated pathway)
 - BID or other stress cause mitochondria to release cytochrome c.
 - cytochrome c bind with Apaf-1 to form the apoptosome.
 - $\bullet~$ Apoptosome $\rightarrow~$ caspase 9 $\rightarrow~$ caspase 3 $\rightarrow~$ cell death.
- Additionally, there is inhibition, cross-talk and feedback mechanisms between the two pathways.

Oligomerization kinetics

Combined model

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Introduction The Biology of Apoptosis: Schematic figure



Zheng 2000, Nat Biotechnology

Oligomerization kinetics

Combined model

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Introduction Existing Models: Overview

Types of Models

Extrinsic

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Oligomerization kinetics

Combined model

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Introduction Existing Models: Overview

Types of Models

- Extrinsic
- Intrinsic

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Introduction Existing Models: Overview

Types of Models

- Extrinsic
- Intrinsic
- Integrated

Oligomerization kinetics

Combined model

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Introduction Existing Models: Overview

Types of Models

- Extrinsic
- Intrinsic
- Integrated
- Note: While many mathematical models describing particular components of the apoptotic pathway exist, these models may be inelegant, limited in scope of a pathway (ie only considering one pathway or activation) or have a complex structure requiring knowledge of numerous biological parameters (which are often estimated).

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Extrinsic

Eissing

THE JOURNAL OF BIOLOGICAL CREMINTRY © 2004 by The American Society for Biochemistry and Molecular Biology, Inc. Vol. 279, No. 35, Issue of August 27, pp. 36892–36897, 2004 Printed in U.S.A.

Bistability Analyses of a Caspase Activation Model for Receptor-induced Apoptosis*

Received for publication, May 3, 2004, and in revised form, June 18, 2004 Published, JBC Papers in Press, June 18, 2004, DOI 10.1074/jbc.M404893200

 $\label{eq:constraint} Thomas Eissing \ref{eq:constraint} State and State an$

From the thantitate for Systems Theory in Engineering. University of Stattgart, Performulating 9, 705500 Stattgart, Germany, the Mantitate for System Domanies and Control, University of Stattgart, Performability 9, 70550 Stattgart, Germany, the Mark Planck Institute for Dynamics of Complex Technical Systems, Sandhornt 1, 39100 Magalebarg. 705095 Stattgart, Cernamy,

Oligomerization kinetics

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Introduction Existing Models: Extrinsic

Eissing





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Introduction	Analysis of caspase modules	Oligomerization kinetics	Combined model	Conclusion 000
Introduct Existing Mod	t ion els: Extrinsic			

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Eissing

• Develop their model based on mass action kinetics.

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Extrinsic

Eissing

- Develop their model based on mass action kinetics.
- Identify the inhibitors of caspase 3 (IAP and its degradation) to be primarily controlling bistable behavior of the death signal.

Oligomerization kinetics

Combined model

Conclusion 000

Introduction Existing Models: Extrinsic

Eissing

- Develop their model based on mass action kinetics.
- Identify the inhibitors of caspase 3 (IAP and its degradation) to be primarily controlling bistable behavior of the death signal.
- *Criticism:* Do not consider the dynamics of the activating stimulus.

Introduction Existing Models: Extrinsic

Eissing

- Develop their model based on mass action kinetics.
- Identify the inhibitors of caspase 3 (IAP and its degradation) to be primarily controlling bistable behavior of the death signal.
- *Criticism:* Do not consider the dynamics of the activating stimulus.
- *Criticism:* This bistability claim is based on parameter adjustments, but is not shown analytically.

Oligomerization kinetics

Combined mode

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Conclusion 000

Introduction Existing Models: Extrinsic

Lai and Jackson

Introduction	Analysis of caspase modules	Oligomerization kinetics	Combined model	Conclusion 000
Introduct Existing Mode	ion ls: Extrinsic			

Lai and Jackson

• Lai and Jackson formulate a mathematical model describing the process of DISC formation and activation.

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Introduction	Analysis of caspase modules	Oligomerization kineti
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Introduction Existing Models: Extrinsic

Lai and Jackson

- Lai and Jackson formulate a mathematical model describing the process of DISC formation and activation.
- Provides a comprehensive model of the receptor trimerization role necessary for apoptosis.

Introduction	Analysis		caspase	modules
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Oligomerization kinetics

Combined model

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Introduction Existing Models: Extrinsic

Lai and Jackson

- Lai and Jackson formulate a mathematical model describing the process of DISC formation and activation.
- Provides a comprehensive model of the receptor trimerization role necessary for apoptosis.
- *Criticism:* The model does not consider the downstream extrinsic pathway.

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Intrinsic

Nakabayashi and <u>Sasaki</u>

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Intrinsic

Nakabayashi and Sasaki

• Nakabayashi and Sasaki explicitly model the formation of the apoptosome as a Apaf-1 heptamer.

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Intrinsic

Nakabayashi and Sasaki

- Nakabayashi and Sasaki explicitly model the formation of the apoptosome as a Apaf-1 heptamer.
- Determine an optimal ratio of cytochrome C and inactive Apaf-1 for the rate of apoptosome formation.

Oligomerization kinetics

Combined model

Conclusion 000

Introduction Existing Models: Intrinsic

Nakabayashi and Sasaki

- Nakabayashi and Sasaki explicitly model the formation of the apoptosome as a Apaf-1 heptamer.
- Determine an optimal ratio of cytochrome C and inactive Apaf-1 for the rate of apoptosome formation.
- *Criticism:* This model focuses only on the apoptosome formation without considering downstream activation of the caspase cascade.

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Intrinsic

Legewie et al

Introduction	Analysis of caspase modules	Oligomerization kinetics	Combined model	Conclusion 000
Introduct Existing Mode	iON ls: Intrinsic			

Legewie et al

• Represent the intrinsic pathway behavior through a system of biochemical equations (28 equations and 33 parameters).

Introduction	Analysis		caspase	modules
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Oligomerization kinetics

Combined model

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Introduction Existing Models: Intrinsic

Legewie et al

- Represent the intrinsic pathway behavior through a system of biochemical equations (28 equations and 33 parameters).
- Identifies inhibitors (IAPs) that mediates bistability and feedback mechanisms of caspase 3 and caspase 9.

Introduction	Analysis		caspase	modules
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Oligomerization kinetics

Combined model

Conclusion 000

Introduction Existing Models: Intrinsic

Legewie *et al*

- Represent the intrinsic pathway behavior through a system of biochemical equations (28 equations and 33 parameters).
- Identifies inhibitors (IAPs) that mediates bistability and feedback mechanisms of caspase 3 and caspase 9.
- *Criticism:* The oligomerization of apoptosome (from Apaf-1 triggered by cytochrome C) is not considered.

Oligomerization kinetics

Combined model

Conclusion 000

Introduction Existing Models: Integrated

Bagci *et al*

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Introduction	Analysis of caspase modules	Oligomerization kinetics	Con
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Introduction Existing Models: Integrated

Bagci et al

• The authors study the role of Bax, Bid and Bcl-2 switching mechanisms as a regulator that ensures bistability in the mitochondria-mediated pathway.

Introduction	Analysis		caspase	modules
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Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Existing Models: Integrated

Bagci et al

- The authors study the role of Bax, Bid and Bcl-2 switching mechanisms as a regulator that ensures bistability in the mitochondria-mediated pathway.
- *Criticism:* The mechanisms employed for activation of the intrinsic pathway does not capture known biological behavior.

Oligomerization kinetics

Combined mode

Conclusion 000

Introduction Novelties of our model: Modularized approach

Modularized Model



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Introduction Novelties of our model: What we did

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Conclusion

Introduction Novelties of our model: What we did

Modularized Model

Integrated the dynamics of previous work as "modules."

• Caspase 8-3

Oligomerization kinetics

Combined mode

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Introduction Novelties of our model: What we did

Modularized Model

- Caspase 8-3
- Formation of DISC

Oligomerization kinetics

Combined model

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Introduction Novelties of our model: What we did

Modularized Model

- Caspase 8-3
- Formation of DISC
- Formation of apoptosome

Oligomerization kinetics

Combined model

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Introduction Novelties of our model: What we did

Modularized Model

- Caspase 8-3
- Formation of DISC
- Formation of apoptosome
- Caspase 9-3

Oligomerization kinetics

Combined model

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Introduction Novelties of our model: What we did

Modularized Model

- Caspase 8-3
- Formation of DISC
- Formation of apoptosome
- Caspase 9-3
- Bid/Bax apoptotic switch

Oligomerization kinetics

Combined model

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Introduction Novelties of our model: What we did

Modularized Model

- Caspase 8-3
- Formation of DISC
- Formation of apoptosome
- Caspase 9-3
- Bid/Bax apoptotic switch
- Inhibitors of caspase (-8, -9, -3)

Oligomerization kinetics

Combined model

Conclusion

Introduction Novelties of our model: What we did

Modularized Model

SCENE 2: SAMIK GHOSH





BISTABILITY IS ALSO PREDICTED. Figure from the Aguda & Friedman book.

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Introduction

Introduction Novelties of our model: What we did

Modularized Model

SCENE 3: KEN HO



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Introduction Novelties of our model: What we did

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SCENE 4: KC TUNG



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Oligomerization kinetics

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Introduction Novelties of our model: What we did

Modularized Model

Integrated the dynamics of previous work as "modules."



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Introduction Novelties of our model: What we did

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Combined mode

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Conclusion 000

Introduction Novelties of our model: What we did

Modularized Model

• Analysis of Caspase Modules

Oligomerization kinetics

Combined mode

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Conclusion 000

Introduction Novelties of our model: What we did

- Analysis of Caspase Modules
- Mathematics of apoptosis activation

Oligomerization kinetics

Combined model

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Conclusion

Introduction Novelties of our model: What we did

- Analysis of Caspase Modules
- Mathematics of apoptosis activation
- Integrated Model and Full System of ODEs

Oligomerization kinetics

Combined model

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Conclusion 000

Introduction Novelties of our model: What we did

- Analysis of Caspase Modules
- Mathematics of apoptosis activation
- Integrated Model and Full System of ODEs
- Simulations and Results

Oligomerization kinetics

Combined model

Conclusion 000

Introduction Novelties of our model: Let the SCREEN PLAY begin

Like every good movie ...



Oligomerization kinetics

Combined model

Conclusion 000

Introduction Novelties of our model: Let the SCREEN PLAY begin

Like every good movie ...

• We role played as individuals, all contributed equally.



Oligomerization kinetics

Combined model

Conclusion

Introduction Novelties of our model: Let the SCREEN PLAY begin

Like every good movie ...

- We role played as individuals, all contributed equally.
- This work was done in very close collaboration.



Oligomerization kinetics

Combined model

Conclusion 000

Introduction Novelties of our model: Let the SCREEN PLAY begin

Like every good movie...

- We role played as individuals, all contributed equally.
- This work was done in very close collaboration.
- Thank you for listening, please sit back and enjoy the rest of the show.



Oligomerization kinetics

Combined mode

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Analysis of caspase modules Extrinsic and intrinsic modules



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Oligomerization kinetics

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Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: Eissing model



Eissing et al. (2004) J Biol Chem 279(35):36892-36897
Oligomerization kinetics

Combined model

Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: basic model

• Basic model: no IAP, only mutual positive feedback of C8 and C3.

Oligomerization kinetics

Combined model

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Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: basic model

• Basic model: no IAP, only mutual positive feedback of C8 and C3.

Equilibrium analysis

- Two steady states: one is $[C3^*] = 0$ (unstable)
- No bistability; sensitive to perturbations

Oligomerization kinetics

Combined model

Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: full Eissing model

• Full model: C8/C3 feedback with IAP and C3*-IAP

Oligomerization kinetics

Combined model

Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: full Eissing model

• Full model: C8/C3 feedback with IAP and C3*-IAP

Equilibrium analysis

- Three steady states: one is $[C3^*] = 0$
- Possible bistability

Oligomerization kinetics

Combined model

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Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: full Eissing model

• Full model: C8/C3 feedback with IAP and C3*-IAP

Equilibrium analysis

- Three steady states: one is $[C3^*] = 0$
- Possible bistability
- For biologically relevant parameters, two other steady states are negative

Oligomerization kinetics

Combined model

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Analysis of caspase modules Extrinsic C8/C3 module: extended Eissing model

• Extended model: additional effect of BAR

 $C8^* + BAR \Longrightarrow C8^*BAR$

Oligomerization kinetics

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Conclusion 000

Analysis of caspase modules Extrinsic C8/C3 module: extended Eissing model

• Extended model: additional effect of BAR

$$C8^* + BAR \Longrightarrow C8^* BAR$$

Equilibrium analysis

- Five steady states: one is $[C3^*] = 0$
- Bistability with three non-negative states for biological parameters
- Intuitively, need thresholds on both C3 and C8



Oligomerization kinetics

Combined model

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Conclusion 000

Analysis of caspase modules Intrinsic C9/C3 module: Legewie model



Wild-type Model Legewie et al. (2006)

Dynamics are similar to Eissing model

Oligomerization kinetics

Combined mode

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Analysis of caspase modules Intrinsic C9/C3 module: bistability through IAP



Oligomerization kinetics

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Oligomerization kinetics Modularization of network



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Oligomerization kinetics

Combined model

Conclusion 000

Oligomerization kinetics DISC module



Oligomerization kinetics

Combined model

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Conclusion 000

Oligomerization kinetics DISC module: formation



Oligomerization kinetics

Combined model

Conclusion

Oligomerization kinetics DISC module: Lai-Jackson model



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Oligomerization kinetics

Combined model

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Conclusion 000

Oligomerization kinetics DISC module: Lai-Jackson solution



Lai R, Jackson TL (2004) Math Biosci Eng 1(2):325-338

Oligomerization kinetics

Combined mode

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Oligomerization kinetics Apoptosome module



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Oligomerization kinetics

Combined mode

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Oligomerization kinetics Apoptosome module: formation



Oligomerization kinetics

Combined mode

Conclusion

Oligomerization kinetics Apoptosome module: Nakabayashi-Sasaki model



Association

$$x_i + x_j \longrightarrow x_{i+j}, i+j \leq 7$$

Dissociation

$$x_k \longrightarrow x_i + x_j, i+j=k$$

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Oligomerization kinetics

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Oligomerization kinetics Apoptosome module: Nakabayashi-Sasaki solution



Nakabayashi J, Sasaki A (2006) J Theor Biol 242:280-287

Oligomerization kinetics

Combined mode

Conclusion 000

Oligomerization kinetics Module abstraction



Oligomerization kinetics

Combined model

Conclusion 000

Combined model Module integration: connection through Bid





Apoptosis and disease: a life or death decision. EMBO Rep. 2004 Jul;5(7):674-8. Epub 2004 Jun 25.

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Oligomerization kinetics

Combined model

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Conclusion 000

Combined model Module integration: Bax oligomerization releases cytochrome *c*



Bid drives this irreversible process.

Oligomerization kinetics

Combined model

Conclusion 000

Combined model Dynamical equations: extrinsic pathway

$$\begin{aligned} [\dot{D}] &= v_1 - \mu_D [D] \\ [\dot{C}8] &= -v_2 + \alpha_{C8} - \mu_{C8} [C8] \\ [\dot{C}8a] &= v_2 - v_{11} - \mu_{C8a} [C8a] \\ [\dot{C}3] &= -v_3 + \alpha_{C3} - \mu_{C3} [C3] \\ [\dot{C}3a] &= v_3 - v_4 - \mu_{C3a} [C3a] \\ [I\dot{A}P] &= -v_4 - v_5 - v_{10} + \alpha_{IAP} - \mu_{IAP} [IAP] \\ [C3aIAP] &= v_4 - \mu_{C3aIAP} [C3aIAP] \\ [B\dot{A}R] &= -v_{11} + \alpha_{BAR} - \mu_{BAR} [BAR] \\ C8aBAR] &= v_{11} - \mu_{C8aBAR} [C8aBAR] \end{aligned}$$

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Oligomerization kinetics

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Conclusion

Combined model Dynamical equations: intrinsic pathway

$$[cytC] = v_7 - v_8 - \mu_{cytC} [cytC]$$
$$[A] = v_8 - \mu_A [A]$$
$$[C9] = -v_9 + \alpha_{C9} - \mu_{C9} [C9]$$
$$[C9a] = v_9 - v_{10} - \mu_{C9a} [C9a]$$
$$C9aIAP] = v_{10} - \mu_{C9aIAP} [C9aIAP]$$
$$[Bid] = -v_6 + \alpha_{Bid} - \mu_{Bid} [Bid]$$
$$C8aBid] = v_6 - \mu_{C8aBid} [C8aBid]$$

Oligomerization kinetics

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Conclusion

Combined model Dynamical equations: modularization

- DISC module: $v_1 = k_1 f_D(l_0, r_0)$
- Bid connection: $v_7 = \frac{k_7 [C8aBid]^{n_7}}{\kappa_{n_7}^{n_7} + [C8aBid]^{n_7}}$
- Apoptosome module: $v_8 = k_8 f_A([cytC], a_0)$



Combined model

Combined model Simulation results: caspase-3 activation is a function of ligand and time



There is a range of ligand that solicits maximum caspase-3 activation.

Transduction of apoptotic signal

Oligomerization kinetics

Combined model

Conclusion 000

Combined model Simulation results: BAR inhibits caspase-8 to prevent accidental activation of apoptosis



Dashed lines: weaken C8*-BAR formation by rate constant: earlier onset. Inhibition of caspase-8 prevents sub-threshold receptor-ligand interaction.

Oligomerization kinetics

Combined model

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Conclusion

Combined model Simulation results: extrinsic pathway alone has limited impact to peak caspase-3 activity



Changing rate constant for activation by caspase-8 (thus extrinsic pathway) did not impact caspase-3 activity.

Oligomerization kinetics

Combined model

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Conclusion 000

Combined model Simulation results: cytochrome *c* amplifies caspase-3 activation



Blocking of cytochrome c release suppresses apoptosis.

Introduction Analysis of caspase modules Oligomerization kinetics Combined model Conclusion

Combined model

Simulation results: caspase-3 activation involves apoptosome assembly and caspase-9



- Reducing rate of apoptosome formation delays onset of caspase-3 activation.
- Caspase-9 activation precedes caspase-3 activation.
- What is the mechanism by which caspase-9 activates caspase-3?

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Oligomerization kinetics

Combined model

Conclusion

Combined model Simulation results: IAP antagonists enhance caspase-3 activation (1)



- In our model, caspase-9 competes for IAP against caspase-3.
- Caspase-9 relieves IAP suppression of caspase-3.
- Real example: Smac mimic potentiates caspase-3 activation. Science 3 September 2004: Vol. 305, no. 5689, pp. 1471–1474

Oligomerization kinetics

Combined model

Conclusion

Combined model Simulation results: IAP antagonists enhance caspase-3 activation (2)



Dashed lines: shut down C9*-IAP formation reaction.

No C9*-IAP, no C3*.

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Oligomerization kinetics

Combined model

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Conclusion ●○○

Conclusion Combined model: demonstrations

- Our model demonstrates:
 - **1** Cytochrome *c* release resembles a point of no return.
 - Connection between extrinsic and intrinsic pathways is required for caspase-dependent cell death.

Oligomerization kinetics

Combined model

Conclusion ○●○

Conclusion Combined model: predictions

• Our model predicts:

- Shutting down intrinsic pathway at cytochrome c release will stop progression to apoptosis.
- Intrinsic pathway feedback (C3, C9, IAP) is a stronger initiator of apoptosis than extrinsic pathway feedback (C3, C8)
- Potential drug targets to induce apoptosis: BAR antagonist, IAP antagonist (Smac mimic: currently under development)



Oligomerization kinetics

Combined model

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Conclusion ○○●

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